

Low energy atmospheric muon neutrinos in MACRO

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We present the measurement of two event samples induced by atmospheric ν_μ of average energy $\bar{E}_\nu \sim 4$ GeV. In the first sample, the neutrino interacts inside the MACRO detector producing an upward-going muon leaving the apparatus. The ratio of the number of observed to expected events is $0.57 \pm 0.05_{stat} \pm 0.06_{syst} \pm 0.14_{theor}$ with an angular distribution similar to that expected from the Bartol atmospheric neutrino flux. The second is a mixed sample of internally produced downward-going muons and externally produced upward-going muons stopping inside the detector. These two subsamples are selected by topological criteria; the lack of timing information makes it impossible to distinguish stopping from downgoing muons. The ratio of the number of observed to expected events is $0.71 \pm 0.05_{stat} \pm 0.07_{syst} \pm 0.18_{theor}$. Using the ratio of the two subsamples (for which most theoretical uncertainties cancel) we can test the pathlength dependence of the oscillation hypothesis. The probability of agreement with the no-oscillation hypothesis is 5%.

The deviations of our observations from the expectations has a preferred interpretation in terms of ν_μ oscillations with maximal mixing and $\Delta m^2 \sim 10^{-3} \div 10^{-2}$ eV². These parameters are in agreement with our results from upward throughgoing muons, induced by ν_μ of much higher energies.

The results from several underground detectors which measure the flux of atmospheric neutrinos give strong indication that ν_μ 's oscillate into neutrinos of another type [1–3]. Fully-contained and partially-contained neutrino-induced events observed in underground detectors come from neutrinos of energy ~ 1 GeV . The flux of atmospheric neutrinos of several tens of GeV can be inferred from the measurement of neutrino-induced upward-going muons that traverse the entire detector (*up-throughgoing muons*). The hypothesis of neutrino oscillations, with best-fit parameters $\sin^2 2\theta_{mix} \sim 1$ and Δm^2 in the range of a few times 10^{-3} eV^2 , can explain the observed anomalies both in the ratio of contained ν_μ to ν_e events (Super-K, Soudan 2) and in the zenith angle distribution of up-throughgoing muons (MACRO, Super-K).

The MACRO detector measures both the high energy (median energy ~ 50 GeV) and few GeV energy atmospheric neutrino fluxes. In Ref. [3,4] the interpretation of the data in terms of ν_μ oscillations came from a deficit and from an anomalous zenith angle distribution of the observed up-throughgoing muons originating from ν_μ interactions in the rock below the detector. Here we report on the measurement of the flux of lower energy ($E_\nu \sim 4$ GeV) atmospheric neutrinos through the detection of ν_μ interactions inside the apparatus (yielding partially contained upgoing and downgoing muons) and by the detection of externally produced upward-going muons stopping inside the detector [5].

MACRO [6] is a large area, modular tracking detector located in Hall B of the Gran Sasso Underground Laboratory in Italy, with an average rock overburden of 3700 hg/cm^2 . It is a rectangular box, 76.6 m \times 12 m \times 9.3 m, divided longitudinally into six supermodules and vertically into a lower part (4.8 m high) and an upper part (4.5 m high). The active detection elements are planes of streamer tubes for tracking and liquid scintillation counters for fast timing. The lower half of the detector is filled with streamer tube planes alternating with trays of crushed rock, which provide most of the 5.3 $kton$ target mass for partially-contained neutrino interactions. The upper part is hollow and contains the electronics racks and work areas. There are 10 horizontal streamer tube planes in the bottom half of the detector, and 4 planes on the top, all with wire and 27° stereo strip readouts. Six vertical planes of streamer tubes cover each side of the detector. The intrinsic angular resolution for muons is between 0.1° and 1.0° depending on the track length. The scintillator system consists of three widely-separated layers of horizontal boxes, and on each vertical side of the detector a layer of vertical boxes inserted between the streamer tubes. The time (position) resolution for muons in a scintillator box is about 500 ps (~ 11 cm). The direction of the muons passing across MACRO is determined by the time-of-flight between two layers of scintillation counters.

The results presented in this letter come from 4.1 live years of data taking with the full detector, from April 1994 to February 1999.

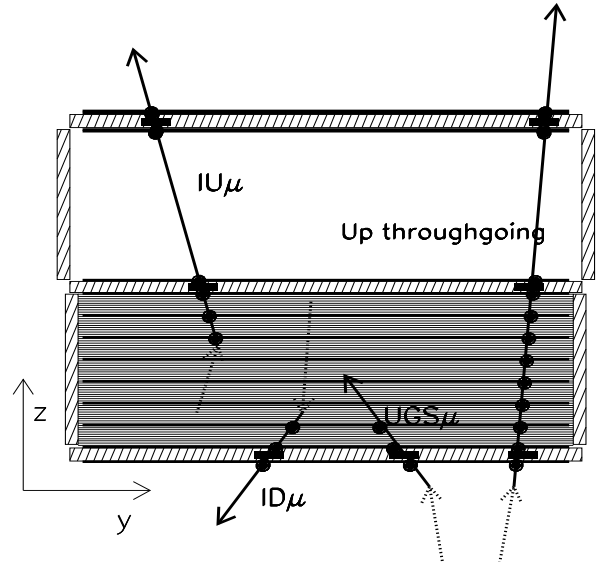


FIG. 1. Event topologies induced by neutrino interactions in or around MACRO. IU = Internal Upgoing μ ; ID = Internal Downgoing μ ; UGS = Upgoing Stopping μ ; Up throughgoing = upward throughgoing μ . The black circles indicate the streamer tube hits, and the black boxes the scintillator hits. The $T.o.F.$ of the muon is measured for the IU and Up throughgoing events.

About 33×10^6 downgoing muons were collected, and were used to monitor the detector efficiency, the running conditions and the acceptance. The trigger rate due to downgoing muons is 0.3 Hz . The trigger efficiency for each scintillation counter and for the streamer tubes was monitored over the data taking period using the downgoing muons.

Two samples of atmospheric muon neutrinos in the few- GeV energy range are measured. In the first sample (up partially-contained or IU =Internal Upgoing μ events) there are (mainly) events induced by charged current (CC) interactions of upgoing ν_μ inside the lower part of MACRO. An upgoing muon is produced, which crosses two scintillation layers (Fig. 1), so that the measurement of the direction is made through time-of-flight.

The second sample is a mix of upgoing and downgoing events. The partially contained downgoing events (down partially-contained or ID =Internal Downgoing μ) are induced by downgoing ν_μ , interacting in the lower part of MACRO. The upgoing stopping events (UGS = Upward Going Stopping muons) are induced by interactions of upgoing ν_μ below the detector yielding an upgoing muon which stops inside the detector. Both the down partially-contained and the upgoing stop events cross only the bottom layer of liquid scintillation counters (see Fig. 1) and are identified by means of topological criteria. The lack of timing information makes it impossible to distinguish between the two subsamples. Fig. 2 shows the parent neutrino energy distribution from a Monte Carlo calculation for the three event topologies detectable in MACRO. The energy spectrum and the median energy of the two samples presented in this letter are almost the same.

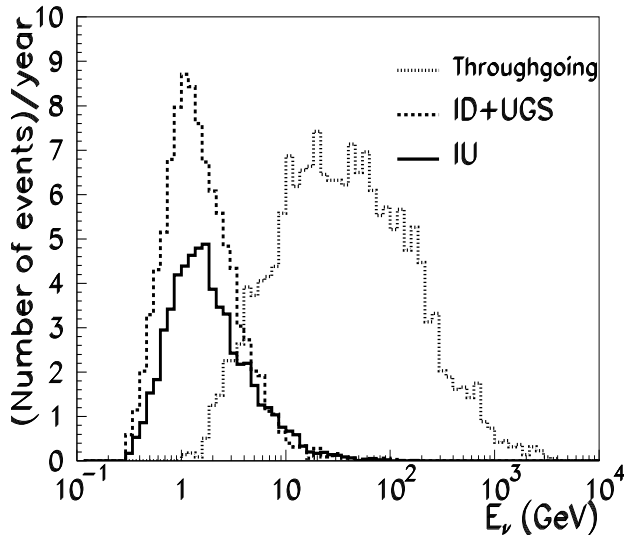


FIG. 2. Monte Carlo simulated distribution of the parent neutrino energy giving rise to the three different topologies of events detectable by MACRO. The distributions are normalized to one year of data taking; the analysis cuts are included.

The identification of *IU* events is based on topological criteria and time-of-flight measurements. The main requirement is the presence of at least two hit scintillator clusters, respectively in the center layer and in the upper part of the apparatus (see Fig. 1). This is the expected topology for a neutrino interacting in the lower detector and producing an upward-going muon with enough energy to exit the apparatus. It is also the topology of the much more numerous downgoing muons stopping in the lower detector. Scintillation timing allows the separation of the two classes of events. Moreover, the scintillators are required to match a streamer tube track reconstructed in space by our standard track-finding algorithms [6]. For *IU* candidates, the lowest point of a track (the starting point) must be inside the apparatus as a condition for the containment of the ν_μ interaction vertex. To reject fake partially-contained events entering from a detector insensitive zone, the extrapolation of the track in the lower part of the detector must geometrically cross and not fire at least one scintillator layer and one streamer tube plane, or at least three planes of streamer tubes. These conditions were tuned on Monte Carlo simulated events, including evaluation of detector inefficiencies. Other cuts are applied to reject background events from downgoing atmospheric muons. They are related to the goodness of the geometrical agreement between scintillator hits and the streamer track, to the proper operation of the scintillation counters and to the quality of the time measurement. The measured $1/\beta$ distribution after all analysis cuts (including the requirements of vertex containment) is shown in Fig. 3. The measured muon velocity βc is evaluated with the sign convention that upgoing muons have $1/\beta \sim -1$. A total of 121 events survive in the range $-1.3 < 1/\beta < -0.7$, which is taken as the range of *IU* signal.

From the time distribution of Fig. 3 one expects some

background events; they are mostly due to wrong time measurements or secondary particle hits, yielding an almost flat $1/\beta$ distribution. The fit of the distribution in the range $-6.0 < 1/\beta < -0.3$ to a gaussian plus a straight line gives an estimated background of 5 events in the signal region. After background subtraction, we have 116 up partially-contained events.

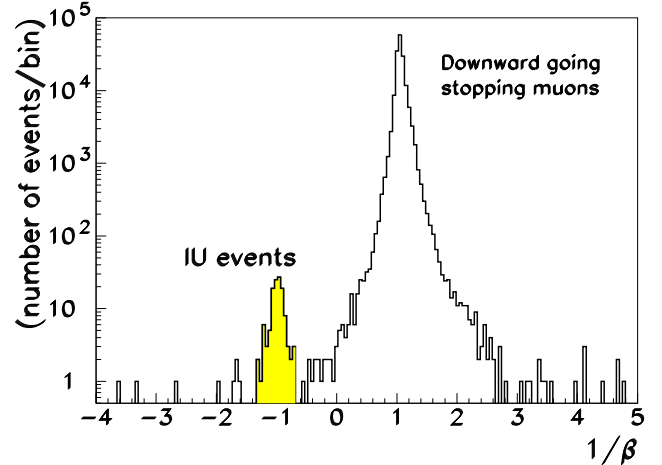


FIG. 3. The $1/\beta$ distribution of partially-contained events after all software cuts. 121 events are in the *IU* event signal region, $-1.3 < 1/\beta < -0.7$, with 5 estimated background events.

The identification of *ID + UGS* events is based on topological criteria. The candidates have a track starting (ending) in the lower apparatus, and crossing the bottom detector face. The track must also be located or oriented in such a way that it could not have entered or exited undetected through insensitive zones in the apparatus. Events with scintillator hits outside the bottom layer, or with the reconstructed track pointing to a detector insensitive zone between modules, are rejected. The standard muon tracking procedure [6] is based on at least four aligned hits in the streamer tubes. This corresponds to a minimum traversed detector thickness $t_v \sim 200 \text{ g/cm}^2$ (*standard sample*). A dedicated retracking procedure was applied to all remaining events. The retracking procedure requires at least three streamer tube hits ($t_v \sim 100 \text{ g/cm}^2$), aligned with respect to a fired scintillation counter in the bottom layer. The number of retracked events is $\sim 5 \times 10^5$ (to be compared with the $\sim 32 \times 10^6$ standard muon tracks); these events follow the same analysis as the standard sample.

After the software cuts, 879 events survive. Some of them are tracked incorrectly (mostly by the retracking), or are bending downgoing muons, entering from a detector insensitive zone. Due to the bending, only a fraction of the streamer tube hits are used by the tracking algorithms. In order to reject these fake candidates, we made a double scan with the MACRO Event Display [6]. To eliminate any bias from the scan procedure, and to evaluate the absolute and relative scanning efficiencies, Monte Carlo (MC) simulated events (described below) were ran-

domly injected into the data sample before the scanning stage. Two physicists independently scanned the merged sample. At the end of the scan, 200 events in the real data (106 $ID + UGS$ candidates are retracted events) are accepted as upgoing stopping or partially contained downgoing muons. 97% of the real events selected by one physicist were also selected by the other.

Downgoing muons which pass near or through the detector may produce low-energy, upgoing particles, which could simulate neutrino-induced upgoing muons if the downgoing muon misses the detector. This background has been evaluated using a full simulation, based on our measurements [7]. The background is 7 ± 2 events. A second background source could arise from atmospheric muons and detector inefficiency. Using a simulated sample of 10^7 atmospheric muons, which includes measured detector inefficiencies, no events were selected by the above described procedure. After background subtraction, 193 events represent the down partially-contained plus upgoing stopping signal.

The expected number of neutrino-induced events was estimated from GMACRO [6], a GEANT-based [8] full MC detector simulation. The ν_e and ν_μ interaction rates have been computed using the atmospheric neutrino flux of the Bartol group [9] and the neutrino cross sections of Ref. [10]. In this cross-section model, the contributions of the exclusive channels of lowest multiplicity (quasi-elastic and single pion production) are calculated separately from deep inelastic scattering (DIS). The DIS contribution to the νN cross section was computed using the GRV-LO-94 [11] parton distribution functions. Using these neutrino fluxes and cross sections for $E_\nu \geq 300$ MeV, we expect a total ($CC + NC$) interaction rate of $71.5 / kton \cdot y$ ($\nu_e + \bar{\nu}_e$) and $148.1 / kton \cdot y$ ($\nu_\mu + \bar{\nu}_\mu$). Two simulated samples have been generated, because of the different vertex locations for the IU and the $ID + UGS$ events; the simulated events were processed with the same analysis chain as the data.

For the IU events, a sample of 10^5 interactions inside the apparatus was generated (equivalent to 85.9 years live time). The simulation indicates (see Table 1) that 87% of detected IU events come from ν_μ charged current (CC) interactions, 9% from ν_e CC and the remaining fraction from neutral current (NC) interactions. Due to detector inefficiencies and analysis algorithm failures, some neutrino-induced events originating in the rock surrounding the detector are expected to contribute to the selected sample of up partially-contained events (upward-throughgoing μ 's appearing as partially-contained). The vertex containment requirements reduce this background to about 1%, evaluated using a simulated sample of up throughgoing muons [3]. The fully-automated selection gives a total number of 202 expected events in the IU event signal region, $-1.3 < 1/\beta < -0.7$ for 4.1 y of live-time.

For the $ID + UGS$ events, 1.16×10^6 neutrino interactions were simulated in a larger volume (including the experimental hall, the detector and the surrounding rock).

The generated events correspond to a live time of 31.1 y . The dimensions of the interaction volume (with 13 m of rock below the detector, and a total rock mass of 165 $kton$ plus 5.3 $kton$ of the apparatus itself) were chosen to reduce to less than 1% the number of ν_μ -induced stopping muons produced outside that volume. The 2199 events which survived the software selection for the $ID + UGS$ were merged with the real events which passed the same software selection, and visually scanned. After the scan procedure 2074 (=94.3%) of the simulated and reconstructed events were accepted, together with the 200 real events. The expected rate is 273 events in 4.1 y live-time. In Table I we give the main features of the IU and $ID + UGS$ simulated samples (expected rate, percentage of CC ν_μ interactions, median parent neutrino energy, and fraction of events induced by upgoing neutrinos).

The number of detected IU events in the 4.1 y live-time is 116, while the expected number is 202. The ratio of the measured to the expected events is $R_{IU} = (\frac{Data}{MC})_{IU} = 0.57 \pm 0.05_{stat} \pm 0.06_{syst} \pm 0.14_{theor}$. For the $ID + UGS$ sample, 193 events are detected while 273 are expected. The ratio is $R_{ID+UGS} = 0.71 \pm 0.05_{stat} \pm 0.07_{syst} \pm 0.18_{theor}$. Each data set is (within errors) consistent with a constant deficit (43% for the IU sample, 29% for the $ID + UGS$) in all zenith bins compared to the Monte Carlo expectations assuming no oscillations. Fig. 4 shows the zenith angle distributions for the two measured data sets and for the Monte Carlo simulations. Due to the analysis cuts and to the apparatus acceptance, there are no events in the last bin of the two distributions. The expectations are affected by a systematic theoretical error due to the uncertainties regarding the atmospheric neutrino flux and the neutrino cross sections. At present there is no unique and reliable estimate of the total theoretical uncertainty for the rate calculations. Each experimental group, and for each event category, has its own way to estimate it. For this analysis we conservatively estimate 20% for the flux and 15% for the cross section, which add in quadrature to an error of 25%. For our high energy events [3] we quoted 17%, while in the recent SuperKamiokande [12] analysis of neutrino-induced stopping muons 22% was quoted.

Our measured value of $R_{IU} = 0.57$ is quite far from its expected value of unity. If we ignored theoretical errors (i.e. if we assumed the flux and cross section as we modeled them were accurate), an experiment with our statistical and experimental uncertainties would only fluctuate so far from unity with probability 2.5×10^{-4} . However, if we take the 25% theoretical error into account, the probability becomes 6.5%. $R_{ID+UGS} = 0.71$ also differs from unity, though not as significantly as R_{IU} .

If the observed deficit were due only to an overall theoretical overestimate of the neutrino flux or cross sections, one would expect $R_{IU} \sim R_{ID+UGS}$ (small differences would remain due to residual geomagnetic effects). Furthermore, the theoretical uncertainties largely cancel if the ratio $IU / ID + UGS$ between the measured number of events is compared with the expectation. The

partial error cancellation arises from the almost identical energy spectra of parent neutrinos for the two samples of events; we evaluated the remaining error as 5%. The experimental systematic uncertainty for the ratio is estimated at 6%. The measured ratio is $\frac{IU}{ID+UGS} = 0.60 \pm 0.07_{stat}$, while the expectation without oscillations is $0.74 \pm 0.04_{sys} \pm 0.04_{theo}$. The probability to obtain a ratio so far from the expected one is 5%, almost independent of the neutrino flux and neutrino cross sections used for the predictions.

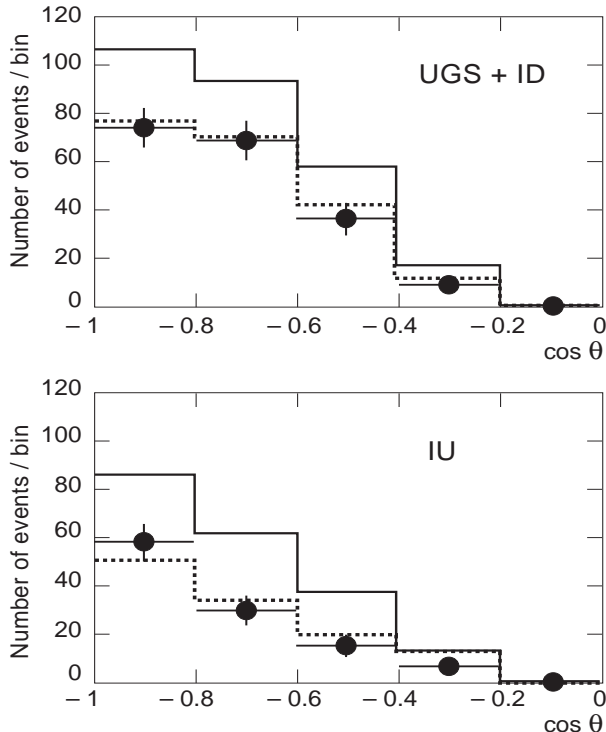


FIG. 4. Measured distributions in the cosine of the zenith angle Θ for the a) $ID + UGS$ and b) IU events (black points with error bars). The solid lines are the Monte Carlo predictions assuming no oscillations. The dashed lines are the expectations for $\nu_\mu \rightarrow \nu_\tau$ oscillations with $\Delta m^2 = 2.5 \times 10^{-3} eV^2$ and maximal mixing.

We investigated if the observed discrepancies between data and expectations could be explained by possible systematic effects. The detector mass is known to $\pm 5\%$. The uncertainty for the detector acceptance was estimated by comparing the shape of the zenith distribution of downward-going muons stopping inside the detector with a MC expectation based on the known rock overburden: the two distributions agree within 6%. Other uncertainties arise from the live-time estimate (3%), the effective containment of the interaction vertex depending on the simulation of the detector response to internal neutrino interactions (4%) and the background subtraction (4%). Adding all these contributions in quadrature yields our quoted experimental systematic uncertainty of 10%, too small to account for the observed discrepancy.

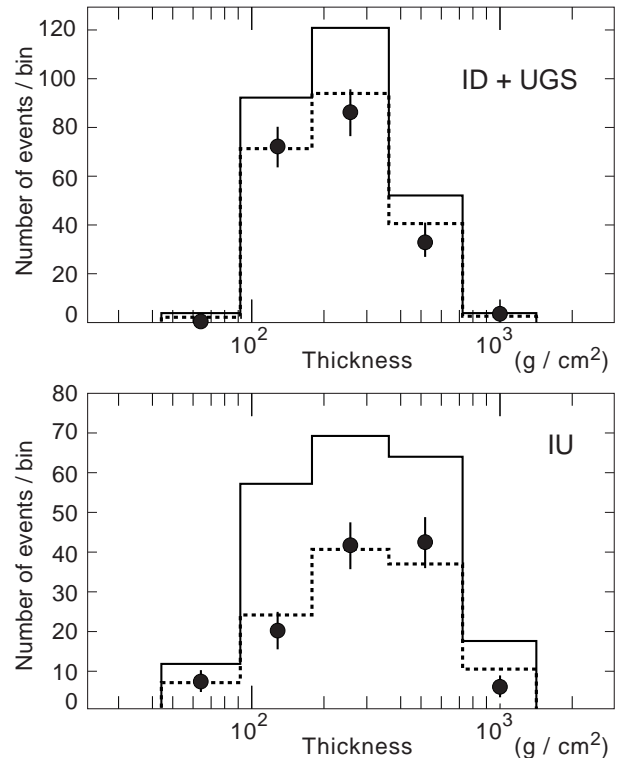


FIG. 5. Distribution of the amount of material (t in $g\ cm^{-2}$) in the detector traversed by IU and $ID + UGS$ events. The data points (black points with error bars) are compared with the Monte Carlo prediction and no oscillations (solid histogram). The expectation for $\nu_\mu \rightarrow \nu_\tau$ oscillations with maximal mixing and $\Delta m^2 = 2.5 \times 10^{-3} eV^2$ is shown by the dashed histogram.

The number of expected events was also evaluated using the NEUGEN neutrino event generator [13] (developed by the Soudan and MINOS collaborations) as input to our MC simulations. The NEUGEN generator predicts $\sim 6\%$ (5%) fewer IU ($ID+UGS$) events than our default generator [10], well within the estimated systematic uncertainty for neutrino cross sections ($\sim 15\%$).

Our data disfavor the no-oscillations hypothesis regardless of overall normalization; they are consistent with neutrino oscillations (ν_μ disappearance) with maximal mixing and $\Delta m^2 \sim (1 \div 20) \times 10^{-3} eV^2$. As a “test point”, we use the best-fit parameters from our high-energy analyses [3,14], $\Delta m^2 = 2.5 \times 10^{-3} eV^2$ and $\sin^2 2\theta_{mix} = 1$. The predicted numbers of events and the angular distributions are indicated by the dashed histograms in Fig. 4; they are in good agreement with the measured data.

For $\Delta m^2 \sim (1 \div 20) \times 10^{-3} eV^2$, upgoing neutrinos (which induce IU and UGS events), which travel thousands of kilometers through the Earth, are reduced by 50%. Almost no reduction is expected for downgoing partially-contained muons. In this scenario, and for a pure ν_μ CC interaction sample, the expected event rate is 1/2 of the IU and 3/4 of the $ID + UGS$ predictions without oscillations. The predicted reduction for upgoing ν_μ is less than 1/2 because of the ν_e and NC event

contaminations. Our data disfavor $\Delta m^2 > 10^{-2} \text{ eV}^2$, for which the ID events are also reduced; both the $ID+UGS$ and IU event rates are $\sim 1/2$ of the no-oscillations expectation. We also disfavor $\Delta m^2 < 10^{-3} \text{ eV}^2$, for which the shape of the angular distributions (Fig. 4) is modified.

Assuming oscillations (with the “test point” parameters) 115 up partially-contained and 202 down partially-contained plus upgoing stopping events are expected. For the IU events, the reduction from the no oscillations hypothesis is 0.57, to be compared with the measured value of $R_{IU} = 0.57$. For the $ID+UGS$ events, it is 0.76, to be compared with $R_{ID+UGS} = 0.71$. The quoted numbers use our default normalization. Recent flux calculations [15] suggest that the Bartol flux which we use may be too high (though within the quoted theoretical error). As far as the event rates are concerned, a lower normalization of the flux can still be partially compensated at low energies by different interaction cross sections for neutrinos.

The event distributions as a function of the muon path-length inside the detector have also been studied, as an independent consistency check. In Fig. 5 the data (black points) are compared with the MC expectation (solid lines for no neutrino oscillations; dashed lines for oscillations at our test point). The shapes are similar, and the data prefer the reduced normalization of the oscillation prediction.

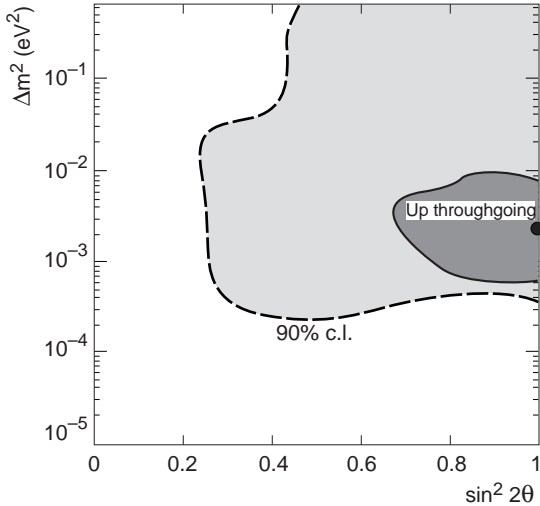


FIG. 6. Allowed contours at 90% C.L. for $\nu_\mu \rightarrow \nu_\tau$ oscillations obtained by combining the low energy neutrino events (IU and $ID + UGS$) using the prescription of [16]. The 90% C.L. contour and the best fit point from our high-energy analysis [14] is also shown as a dashed line.

We estimated the most likely values of Δm^2 and $\sin^2 2\theta_{mix}$ using a χ^2 method for data and Monte Carlo for the data of Fig. 4. The χ^2 was computed with ten degrees of freedom: the histograms (2×4 bins, normalized so as to contain only distribution shape information), the $\frac{IU}{ID+UGS}$ ratio and the overall normalization. The statistical and systematic errors are added in quadrature;

the systematic uncertainty is 10% in each bin of the angular distributions, 5% for the ratio, and 25% for the normalization. Fig. 6 shows the 90% confidence level region, based on the application of the MC prescriptions of Ref. [16] on a $(\sin^2 2\theta_{mix}, \Delta m^2)$ grid. The expected flux Φ_{osc}^i for a given point of $(\sin^2 2\theta_{mix}, \Delta m^2)$ in the grid is obtained by weighting each simulated event with its surviving probability $P(\nu_\mu \rightarrow \nu_\mu) = 1 - \sin^2 2\theta_{mix} \cdot \sin^2(1.27 \cdot \Delta m^2 L/E_\nu)$ in that bin. The maximum of the χ^2 probability (97%) occurs at $\sin^2 2\theta_{mix} = 1.0$; this χ^2 probability is almost constant in the interval $\Delta m^2 = (1 \div 20) \times 10^{-3} \text{ eV}^2$. In the region of the maximum, the flux normalization factor is 1.02 in both data sets (i.e. the data are 2% higher than the oscillated predictions with our normalization).

In conclusion, we presented measurements of two samples of events induced by relatively low-energy neutrinos ($\bar{E}_\nu \sim 4 \text{ GeV}$) interacting in MACRO or in the surrounding rock. The neutrinos originate from cosmic ray interactions in the upper atmosphere above the detector (downgoing events) or up to $\sim 13000 \text{ km}$ away on the opposite side of the Earth (upgoing events). The ratio of the number of observed to expected events (no oscillations) is $0.57 \pm 0.05_{stat} \pm 0.06_{syst} \pm 0.14_{theor}$ for the IU events and $0.71 \pm 0.05_{stat} \pm 0.07_{sys} \pm 0.18_{theo}$ for the $ID + UGS$. Within statistics, the observed deficits are uniform over the zenith angle. From the ratio of IU to $ID + UGS$, the probability that there is an overall reduction in the number of neutrino-induced muons is 5%. The hypothesis of muon neutrino oscillations explains the different deficits in IU and $ID + UGS$ events with higher probability. The large theoretical uncertainties for the neutrino flux and cross sections is dominant in each data set; the ratio of the two low energy samples is dominated by statistical uncertainties. The regions with $\Delta m^2 > 3 \times 10^{-4} \text{ eV}^2$ and $\sin^2 2\theta_{mix} > 0.25$ are allowed at 90% C.L. The best region corresponds to maximal mixing and $\Delta m^2 = (1 \div 20) \times 10^{-3} \text{ eV}^2$. This result confirms the scenario proposed by the measurement of higher-energy neutrino-induced muons by MACRO [3,14], as well as by other experiments [1,2], all of which favor the ν_μ oscillation hypothesis with maximal mixing and Δm^2 of a few times 10^{-3} eV^2 .

	Rate (<i>ev/y</i>)	ν_μ CC (%)	\bar{E}_ν (GeV)	$\nu \uparrow$ (%)
IU	49.3	87	4.2	94
ID+UGS	66.7	87	3.5	51

TABLE I. Summary of the properties of simulated IU and $ID + UGS$ events. From column 2 to 5: expected event rate (no neutrino oscillations); percentages of events induced by ν_μ CC interactions; median parent neutrino energies (5% of events with the highest/lowest energies were excluded); percentages of events induced by upgoing neutrinos.

We acknowledge the support of the staff of the Gran Sasso Laboratory and of the Institutions participating in the experiment. We thank the Istituto Nazionale di Fisica Nucleare (INFN), the U.S. Department of Energy and the U.S. National Science Foundation for their support. We thank INFN, FAI, ICTP (Trieste), NATO and WorldLab for providing fellowships and grants for non-Italian citizens.

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